

**QUESTION:** What is the number of zeroes at the end of the product  
 $1002 \times 1004 \times 1006 \times 1008 \times \dots \times 1300$ ?

**OPTIONS:**

- a) 37
- b) 38
- c) 165
- d) None of these

**SOLUTION:** It can be written as

$$2(501 \times 502 \times 503 \times 504 \times \dots \times 650)$$

$$\text{or } \frac{2 \times 650!}{500!}$$

Now, to determine the number of zeroes, we have to determine the power of 10.

$$\Rightarrow \frac{2 \times 650!}{500! \times 10^M}$$

$$\begin{array}{r|l} 5 & 650 \\ \hline 5 & 130 \\ \hline 5 & 26 \\ \hline 5 & 5 \\ \hline & 1 \end{array} \left. \vphantom{\begin{array}{r|l} 5 & 650 \\ \hline 5 & 130 \\ \hline 5 & 26 \\ \hline 5 & 5 \\ \hline & 1 \end{array}} \right\} \text{Add} = 162$$

$$\begin{array}{r|l} 5 & 500 \\ \hline 5 & 100 \\ \hline 5 & 20 \\ \hline & 4 \end{array} \left. \vphantom{\begin{array}{r|l} 5 & 500 \\ \hline 5 & 100 \\ \hline 5 & 20 \\ \hline & 4 \end{array}} \right\} \text{Add} = 124$$

Since power of 5 will always be less than that of power of 2, therefore we will be concerning with the power of 5 only. Now expressing  $\frac{2 \times 650!}{500! \times 5^M}$  in terms of

power of 5, we get  $\frac{N \cdot 5^{162}}{5^{124} \times 5^M}$

This gives  $M = 38$

So, total number of zeroes at the end of the product  $1002 \times 1004 \times \dots \times 1300$  is 38.